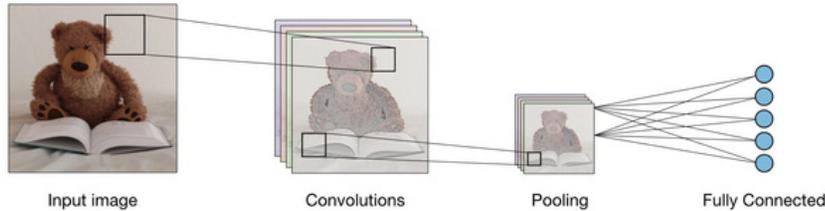


VIP Cheatsheet: Convolutional Neural Networks



Overview

Architecture of a traditional CNN – Convolutional neural networks, also known as CNNs, are a specific type of neural networks that are generally composed of the following layers:



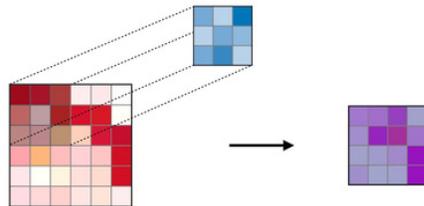
The convolution layer and the pooling layer can be fine-tuned with respect to hyperparameters that are described in the next sections.

Filter hyperparameters

Types of layer The convolution layer contains filters for which it is important to know the meaning behind its hyperparameters.

Convolutional layer (CONV) – The convolution layer (CONV) uses filters that perform

convolution operations as it is scanning the input I with respect to its dimensions. Its hyperparameters include the filter size F and stride S . The resulting output O is called *feature map* or output feature map (also called *activation map*) of size $O \times O \times 1$.

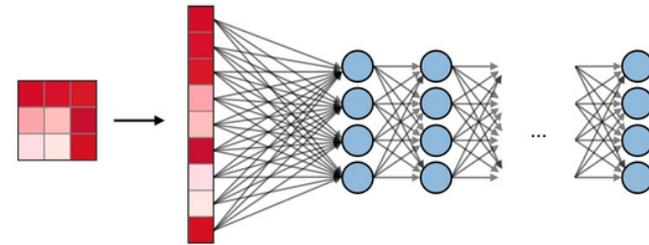


Remark: the convolution step can be generalized to the 1D and 3D cases as well.

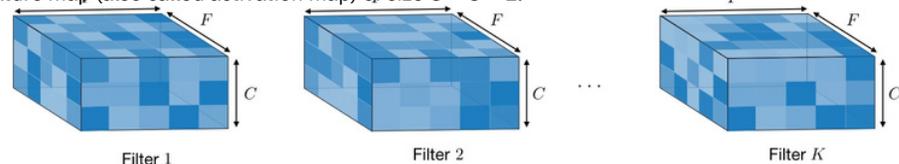
Pooling (POOL) – The pooling layer (POOL) is a downsampling operation, typically applied after a convolution layer, which does some spatial invariance. In particular, max and average pooling are special kinds of pooling where the maximum and average value is taken, respectively.

	Max pooling	Average pooling
Purpose	Each pooling operation selects the maximum value of the current view	Each pooling operation averages the values of the current view
Illustration		
Comments	- Preserves detected features - Downsamples feature map - Most commonly used	- Used in LeNet

Fully Connected (FC) – The fully connected layer (FC) operates on a flattened input where each input is connected to all neurons. If present, FC layers are usually found towards the end of CNN architectures and can be used to optimize objectives such as class scores.



Dimensions of a filter – A filter of size $F \times F \times C$ applied to an input containing C channels is a $F \times F \times C$ volume that performs convolutions on an input of size $I \times I \times C$ and produces an output feature map of size $O \times O \times 1$.



Remark: the application of K filters of size $F \times F \times C$ results in an output feature map of size $O \times O \times K$.

Stride – For a convolutional or a pooling operation, the stride S denotes the number of pixels by which the window moves after each operation.



Zero-padding – Zero-padding denotes the process of adding P zeroes to each side of the boundaries of the input. This value can either be manually specified or automatically set through one of the three modes detailed below:

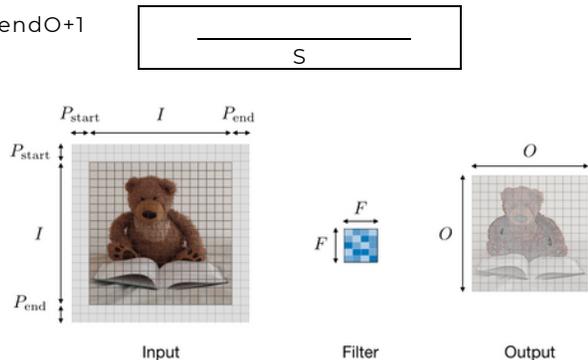
Valid Same Full

$O = \lfloor \frac{I - F + 2P}{S} + 1 \rfloor$ $P \in \{0, 1\}$ Value $P=0$ $O = \lfloor \frac{I - F + 1}{S} \rfloor$			
Illustration			
Purpose	<ul style="list-style-type: none"> - No padding - Drops last convolution if dimensions do not match 	<ul style="list-style-type: none"> - Padding such that feature map size has size $\lceil \frac{I}{S} \rceil$ - Output size is mathematically convenient - Also called 'half padding' 	<ul style="list-style-type: none"> - Maximum padding such that end convolutions are applied on the limits of the input - Filter 'sees' the input end-to-end

Tuning hyperparameters

Parameter compatibility in convolution layer – By noting I the length of the input volume size, F the length of the filter, P the amount of zero padding, S the stride, then the output size O of the feature map along that dimension is given by:

$$O = \lfloor \frac{I - F + P_{start} + P_{end}}{S} + 1 \rfloor$$



Remark: often times, $P_{start} = P_{end} = P$, in which case we can replace $P_{start} + P_{end}$ by $2P$ in the formula above.

Understanding the complexity of the model – In order to assess the complexity of a model, it is often useful to determine the number of parameters that its architecture will have. In a given layer of a convolutional neural network, it is done as follows:

	CONV	POOL	FC
Illustration			
Input size	I I C	I I C	N_{in}
Output size	O O K	O O	N_{out}
Number of parameters	F C K	C	t

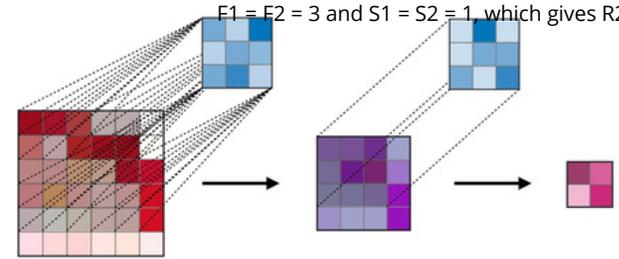
Remarks - In most cases, $S < F$ done channel-wise per neuron
 - The number of FC
 - A common choice - In most cases, $S = F$ neurons is free of structural constraints
 - One bias parameter
 - Input is flattened
 - Pooling operation - One bias parameter

Receptive field – The receptive field at layer k is the area denoted R_k

R_k of the input that each pixel of the k-th activation map can 'see'. By calling F_j the filter size of layer j and S_j the stride value of layer j and with the convention $S_0 = 1$, the receptive field at layer k can be computed with the formula:

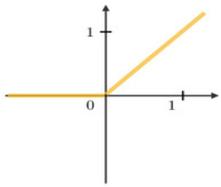
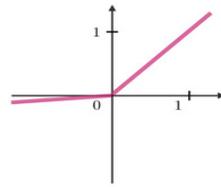
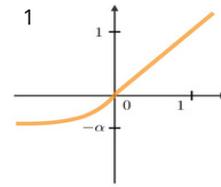
$$R_k = 1 + (F_j - 1) \prod_{i=0}^{j-1} S_i$$

In the example below, we have $F_1 = F_2 = 3$ and $S_1 = S_2 = 1$, which gives $R_2 = 1 + 2 \cdot 1 + 2 \cdot 1 = 5$.



Commonly used activation functions

Rectified Linear Unit – The rectified linear unit layer (ReLU) is an activation function g that is used on all elements of the volume. It aims at introducing non-linearities to the network. Its variants are summarized in the table below:

ReLU	Leaky ReLU	ELU
$g(z) = \max(0, z)$	$g(z) = \max(\epsilon z, z)$ with ϵ	$g(z) = \max(\alpha(ez - 1), z)$ with α
		
Non-linearity complexities biologically interpretable	Addresses negative values issue for negative values	Differentiable everywhere

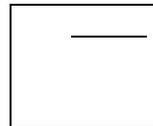
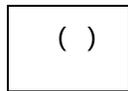
Non-linearity
complexities
biologically
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Addresses
negative
values
issue
for
negative
values

Differentiable
everywhere

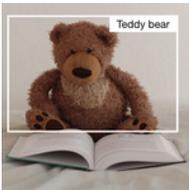
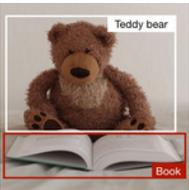
Softmax – The softmax step can be seen as a generalized logistic function that takes as input a vector of scores $x \in \mathbb{R}^n$ and outputs a vector of output probabilities $p \in \mathbb{R}^n$ through a softmax function at the end of the architecture. It is defined as follows:

$$p_j = \frac{e^{x_j}}{\sum_{i=1}^n e^{x_i}}$$

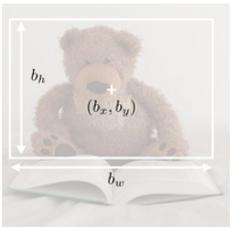
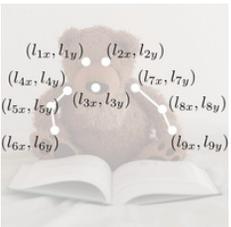


Object detection

Types of models – There are 3 main types of object recognition algorithms, for which the nature of what is predicted is different. They are described in the table below:

Image classification	Classification with localization	Detection
		
- Classifies a picture - Predicts probability of a picture	- Detects object in a picture - Predicts probability of object and where it is	- Detects up to several objects - Predicts probabilities of objects and where they are located
Traditional CNN	Simplified YOLO, R-CNN	YOLO, R-CNN

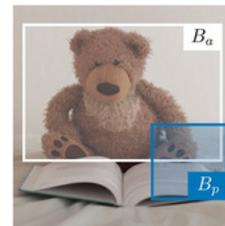
Detection – In the context of object detection, different methods are used depending on whether we just want to locate the object or detect a more complex shape in the image. The two main ones are summed up in the table below:

Bounding box detection	Landmark detection
Detects the part of the image where the object is located	- Detects a shape or characteristics of an object (e.g. eyes) - More granular
	
Box of center (b_x, b_y) , height b_h and width b_w	Reference points (l_x, l_y)

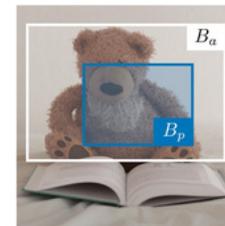
Box of center (b_x, b_y) , height b_h and width b_w

Intersection over Union – Intersection over Union, also known as IoU, is a function that quantifies how correctly positioned a predicted bounding box B_p is over the actual bounding box B_a . It is defined as:

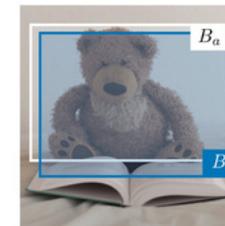
$$IoU(B_p, B_a) = \frac{|B_p \cap B_a|}{|B_p \cup B_a|}$$



$$IoU(B_p, B_a) = 0.1$$



$$IoU(B_p, B_a) = 0.5$$



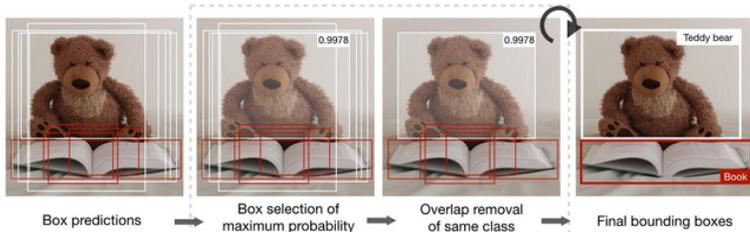
$$IoU(B_p, B_a) = 0.9$$

Remark: we always have $IoU \in [0, 1]$. By convention, a predicted bounding box B_p is considered as being reasonably good if $IoU(B_p, B_a) > 0.5$.

Anchor boxes – Anchor boxing is a technique used to predict overlapping bounding boxes. In practice, the network is allowed to predict more than one box simultaneously, where each box prediction is constrained to have a given set of geometrical properties. For instance, the first prediction can potentially be a rectangular box of a given form, while the second will be another rectangular box of a different geometrical form.

Non-max suppression – The non-max suppression technique aims at removing duplicate overlapping bounding boxes of a same object by selecting the most representative ones. After having removed all boxes having a probability prediction lower than 0.6, the following steps are repeated while there are boxes remaining:

- Step 1: Pick the box with the largest prediction probability.
- Step 2: Discard any box having an $IoU > 0.5$ with the previous box.



YOLO – You Only Look Once (YOLO) is an object detection algorithm that performs the following steps:

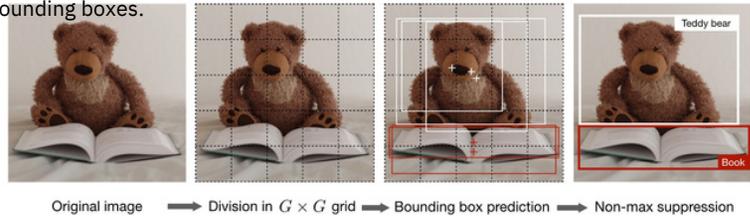
- Step 1: Divide the input image into a $G \times G$ grid.
- Step 2: For each grid

[cell, run a CNN that predicts of the following form:
 $y = \{c, x, y, w, h, p\}$, where c is the class, x, y, w, h are the bounding box properties, and p is the probability of detecting an object.

p , ... \in repeated k times

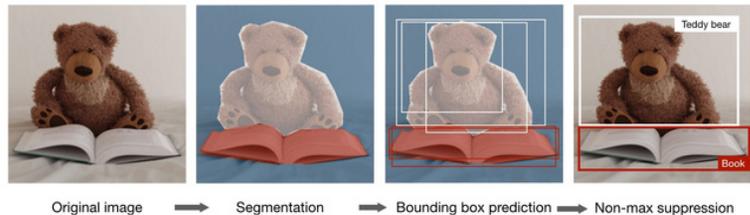
where p_c is the probability of detecting an object, b_x, b_y, b_h, b_w are the properties of the detected bounding box, c_1, \dots, c_p is a one-hot representation of which of the p classes were detected, and k is the number of anchor boxes.

- Step 3: Run the non-max suppression algorithm to remove any potential duplicate overlapping bounding boxes.



Remark: when $p_c = 0$, then the network does not detect any object. In that case, the corresponding predictions b_x, \dots, c_p have to be ignored.

R-CNN – Region with Convolutional Neural Networks (R-CNN) is an object detection algorithm that first segments the image to find potential relevant bounding boxes and then run the detection algorithm to find most probable objects in those bounding boxes.



Remark: although the original algorithm is computationally expensive and slow, newer architectures enabled the algorithm to run faster, such as Fast R-CNN and Faster R-CNN.

Face verification and recognition

Types of models – Two main types of model are summed up in table below:

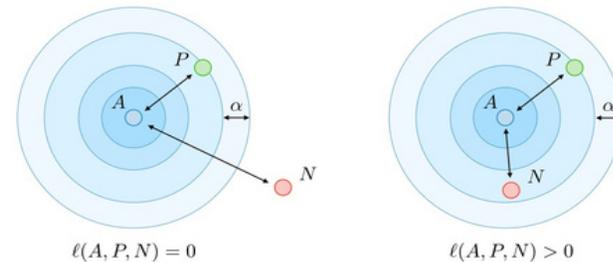
	Face verification	Face recognition
Question	- Is this the correct person?	- Is this one of the K persons in the database?
Lookup	- One-to-one lookup	- One-to-many lookup
Diagram		

One Shot Learning – One Shot Learning is a face verification algorithm that uses a limited training set to learn a similarity function that quantifies how different two given images are. The similarity function applied to two images is often noted $d(\text{image 1}, \text{image 2})$.

Siamese Network – Siamese Networks aim at learning how to encode images to then quantify how different two images are. For a given input image $x(i)$, the encoded output is often noted as $f(x(i))$.

Triplet loss – The triplet loss ℓ is a loss function computed on the embedding representation of a triplet of images A (anchor), P (positive) and N (negative). The anchor and the positive example belong to a same class, while the negative example to another one. By calling $\alpha \in \mathbb{R}^+$ the margin parameter, this loss is defined as follows:

$$\ell(A, P, N) = \max(d(A, P) - d(A, N) + \alpha, 0)$$



Neural style transfer

Motivation – The goal of neural style transfer is to generate an image G based on a given content C and a given style S .



Activation – In a given layer l , the activation is noted $a[l]$ and is of dimensions $n \times n_w \times n_c$

Content cost function – The content cost function $J_{content}(C,G)$ is used to determine how the generated image G differs from the original content image C . It is defined as follows:

$$J_{content}(C,G) = \frac{1}{2} \|a[l](C) - a[l](G)\|_2^2$$

Style matrix – The style matrix $G[l]$ of a given layer l is a Gram matrix where each of its elements $G[l]_{kk'}$ quantifies how correlated the channels k and k' are. It is defined with respect to activations $a[l]$ as follows:

$$G[l]_{kk'} = \frac{1}{n} \sum_i a[l]_{ki} a[l]_{k'i}$$

Remark: the style matrix for the style image and the generated image are noted $G[l](S)$ and $G[l](G)$ respectively.

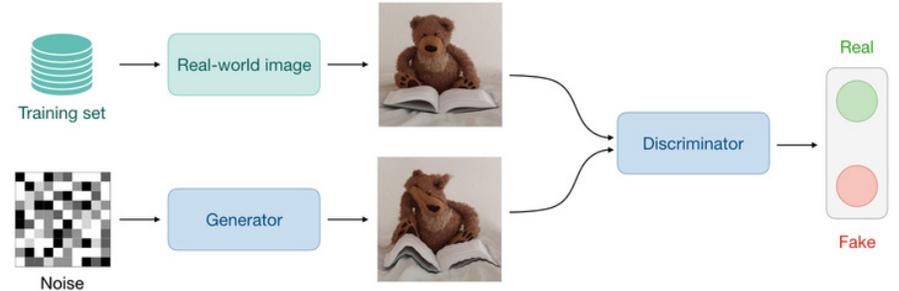
Style cost function – The style cost function $J_{style}(S,G)$ is used to determine how the generated image G differs from the style S . It is defined as follows:

$$J_{style}(S,G) = \frac{1}{2} \|G[l](S) - G[l](G)\|_F^2 = \frac{1}{2} \sum_{k,k'} (G[l]_{kk'}(S) - G[l]_{kk'}(G))^2$$

Overall cost function – The overall cost function is defined as being a combination of the content and style cost functions, weighted by parameters α, β , as follows:

$$J(G) = \alpha J_{content}(C,G) + \beta J_{style}(S,G)$$

Remark: a higher value of α will make the model care more about the content while a higher value of β will make it care more about the style.



Remark: use cases using variants of GANs include text to image, music generation and synthesis.

ResNet – The Residual Network architecture (also called ResNet) uses residual blocks with a high number of layers meant to decrease the training error. The residual block has the following characterizing equation:

$$a[t+2] = g(a[t] + z[t+2])$$

Inception Network – This architecture uses inception modules and aims at giving a try at different convolutions in order to increase its performance. In particular, it uses the 1×1 convolution trick to lower the burden of computation.

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